Products of CW complexes

Andrew Brooke-Taylor

CW complexes are used extensively in algebraic topology as a suitable class of spaces to work with, but the product of two CW complexes need not be a CW complex, as shown by Dowker. Whitehead and Milnor gave sufficient conditions on the two spaces for the product to be a CW complex, and in 1978 Liu gave a characterisation under the assumption of CH of those pairs of CW complexes for which the product is a CW complex. In a 1982 paper Tanaka weakened the assumption for this characterisation to $\mathfrak{b}=\aleph_1$, but it seems the topic has remained unaddressed since then. In this talk I will present a complete characterisation, valid under ZFC alone, of those pairs of CW complexes whose product is a CW complex.